

$$f(x) = x^3 + k \ln x \quad (k \in \mathbb{R}) \quad f'(x) = 3x^2 + \frac{k}{x}$$

$$k = 6$$

$$y = f(x) \quad (1, f(1))$$

$$g(x) = f(x) - f(x) = \frac{9}{x}$$

$$k = 3$$

$$x_1, x_2 \in [1, \infty) \quad x_1 < x_2$$

$$\frac{f(x_1) - f(x_2)}{2} = \frac{f(x_1) - f(x_2)}{x_1 - x_2}$$

$$y = 9x - 8$$

$$g(x) = 9x - 8 \quad 0,1 \quad 1,$$

$$g(x) = 9x - 8 \quad g(1) = 1$$

$$f(x) = x^3 + k \ln x \quad f'(x) = 3x^2 + \frac{k}{x}$$

$$x_1, x_2 \in [1, \infty) \quad x_1 < x_2 \quad \frac{x_1}{x_2} = t \quad (t > 1)$$

$$x_1 - x_2 = f(x_1) - f(x_2) = 2 \frac{f(x_1) - f(x_2)}{x_1 - x_2}$$

$$x_1 - x_2 = 3x_1^2 \frac{k}{x_1} - 3x_2^2 \frac{k}{x_2} = 2 \frac{x_1^3 - x_2^3}{x_1 - x_2} + k \ln \frac{x_1}{x_2}$$

$$x_1^3 - x_2^3 - 3x_1^2x_2 - 3x_1x_2^2 - k \frac{x_1}{x_2} - \frac{x_2}{x_1} - 2k \ln \frac{x_1}{x_2}$$

$$x_2^3 - t^3 - 3t^2 - 3t - 1 - k - t - \frac{1}{t} - 2 \ln t$$

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$$\frac{3x_1^2 \frac{k}{x_1} + 3x_2^2 \frac{k}{x_2}}{2} - \frac{x_1^3 - x_2^3 - k \ln \frac{x_1}{x_2}}{x_1 - x_2}$$

$$\frac{3}{2} x_1^2 - x_2^2 - \frac{k}{2} \frac{x_1 - x_2}{x_1 x_2} - x_1^2 + x_1 x_2 + x_2^2 + k \frac{\ln x_1 - \ln x_2}{x_1 - x_2}$$

$$x_1 - x_2 - 3k \frac{x_1^2 - x_2^2}{x_1 x_2} - 2k \ln \frac{x_1}{x_2}$$

$$t - x_1 - x_2 - 1 - g t - t - x_2^3 - k \frac{1}{x_2} t - x_2 \frac{1}{t} - 2k \ln t - 2k \ln x_2$$

$$g' t - 3 t - x_2^2 - k \frac{1}{x_2} - x_2 \frac{1}{t^2} - \frac{2k}{t} - 3 t - x_2^2 - k \frac{t - x_2^2}{x_2 t^2} - \frac{t - x_2^2 - 3t^2 x_2 - k}{x_2 t^2} = 0$$

$$g t - x_2, \quad g t - g x_2 = 0$$

$$x_1 - x_2 - 3k \frac{x_1^2 - x_2^2}{x_1 x_2} - 2k \ln \frac{x_1}{x_2}$$

$$t - x_1 - t - g t - g x_2 = 0$$

$$g t - g x_2$$

$$x_1 - x_2 - 3k \frac{x_1^2 - x_2^2}{x_1 x_2} - 2k \ln \frac{x_1}{x_2}$$

$$\frac{x_1}{x_2} - x_1 - x_2 - \frac{x_1 - x_2}{x_2} - \frac{x_1}{x_2} - 1$$

$$\frac{x_1}{x_2} - 1 - 3k \frac{x_1 - x_2}{x_2 x_1} - 2k \ln \frac{x_1}{x_2} = 0$$

$$t - \frac{x_1}{x_2} - 1 - h t - t - 1^3 - k(t - \frac{1}{t}) - 2k \ln t$$

$$h' t - 3 t - 1^2 - k(1 - \frac{1}{t^2}) - k \frac{2}{t} - \frac{t - 1^2 - 3t^2 - k}{t^2} = 0$$

$$h t - 1, \quad h t - h - 1 = 0$$

$$x_1 - x_2 - 3k \frac{x_1^2 - x_2^2}{x_1 x_2} - 2k \ln \frac{x_1}{x_2}$$

$$\frac{x_1}{x_2} - x_1 - x_2 - \frac{x_1}{x_2} - 1$$

$$\frac{x_1}{x_2} = 1 + k \frac{x_1}{x_2} - \frac{x_2}{x_1} - 2k \ln \frac{x_1}{x_2} = 0$$

$$f(x) = e^{mx} - x^2 - mx$$

$$f(x) = (x, 0) \quad (0, )$$

$$x_1, x_2 \in [1, 1] \quad |f(x_1) - f(x_2)| = e - 1 - m$$

$$f(x) = (x - 2)e^x - a(x - 1)^2$$

$a$

$$x_1, x_2 \in f(x)$$

$$x_1, x_2 \in 2$$